

Fig. 3-1 Two-variable Map

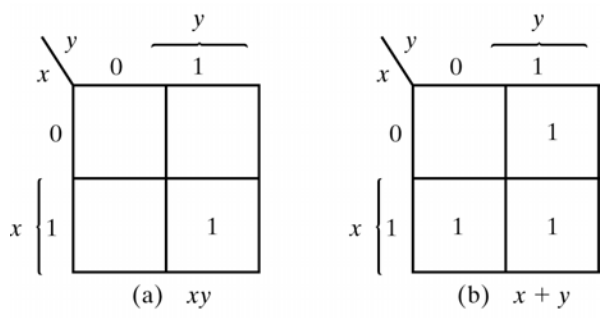


Fig. 3-2 Representation of Functions in the Map

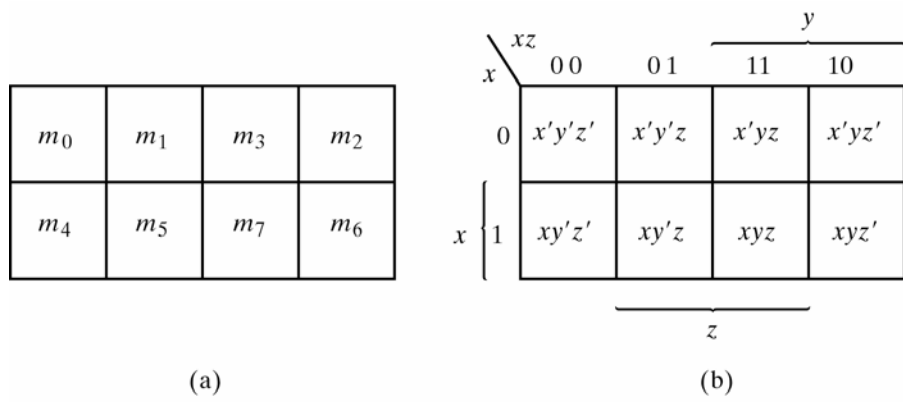


Fig. 3-3 Three-variable Map

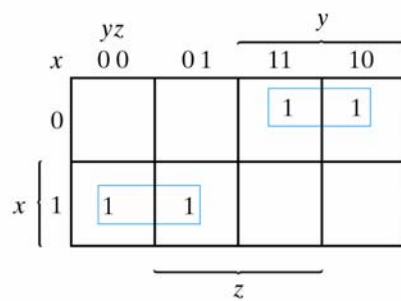


Fig. 3-4 Map for Example 3-1; $F(x, y, z) = \Sigma(2, 3, 4, 5) = x'y + xy'$

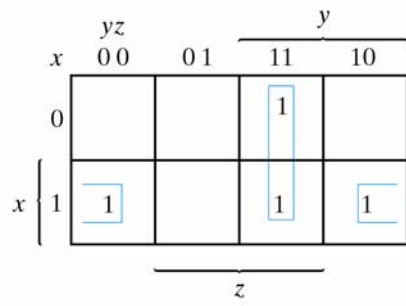


Fig. 3-5 Map for Example 3-2; $F(x, y, z) = \Sigma(3, 4, 6, 7) = yz + xz'$

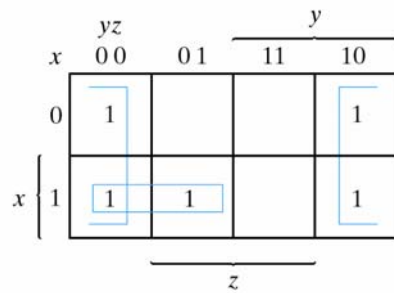


Fig. 3-6 Map for Example 3-3; $F(x, y, z) = \Sigma(0, 2, 4, 5, 6) = z' + xy'$

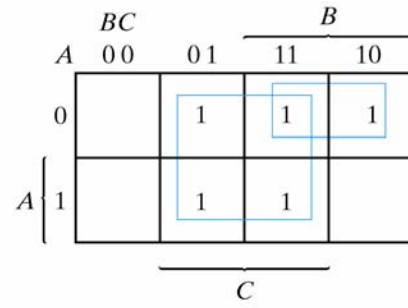


Fig. 3-7 Map for Example 3-4; $A'C + A'B + AB'C + BC = C + A'B$

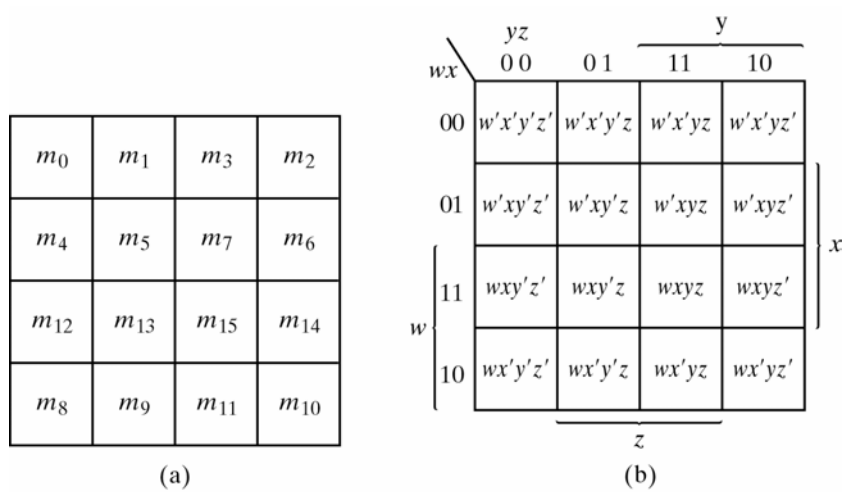


Fig. 3-8 Four-variable Map

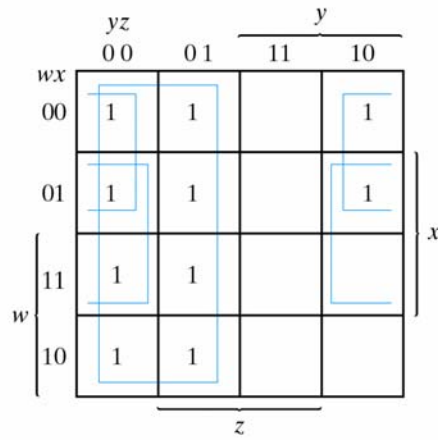


Fig. 3-9 Map for Example 3-5; $F(w, x, y, z)$
 $= \Sigma (0, 1, 2, 4, 5, 6, 8, 9, 12, 13, 14) = y' + w'z' + xz'$

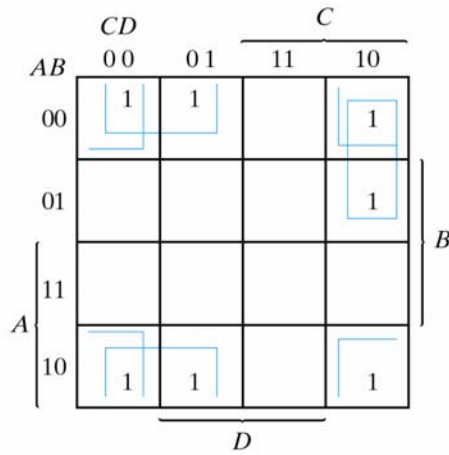


Fig.3-10 Map for Example 3-6; $A'B'C + B'CD' + A'BCD'$
 $+ AB'C' = B'D' + B'C' + A'CD'$

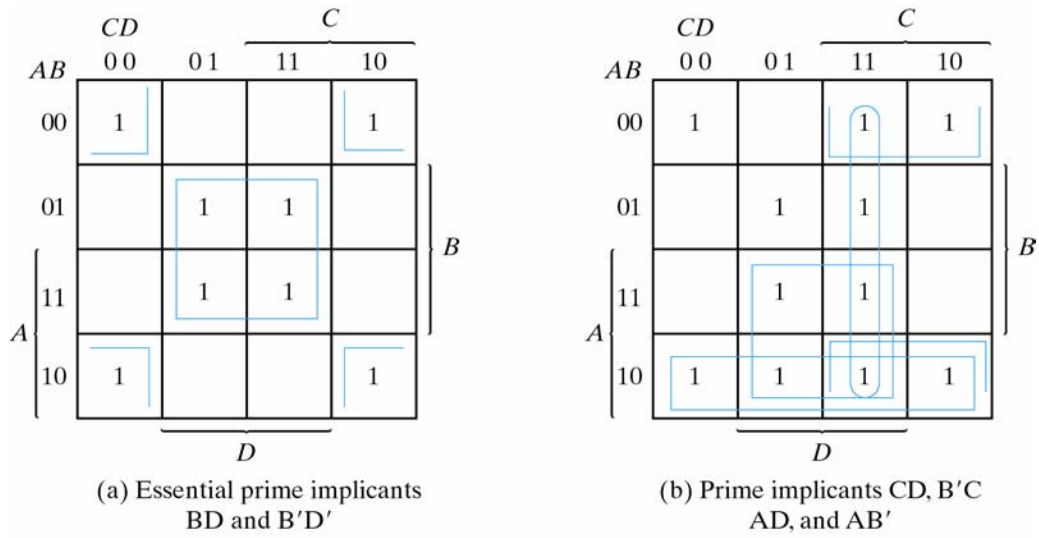


Fig. 3-11 Simplification Using Prime Implicants

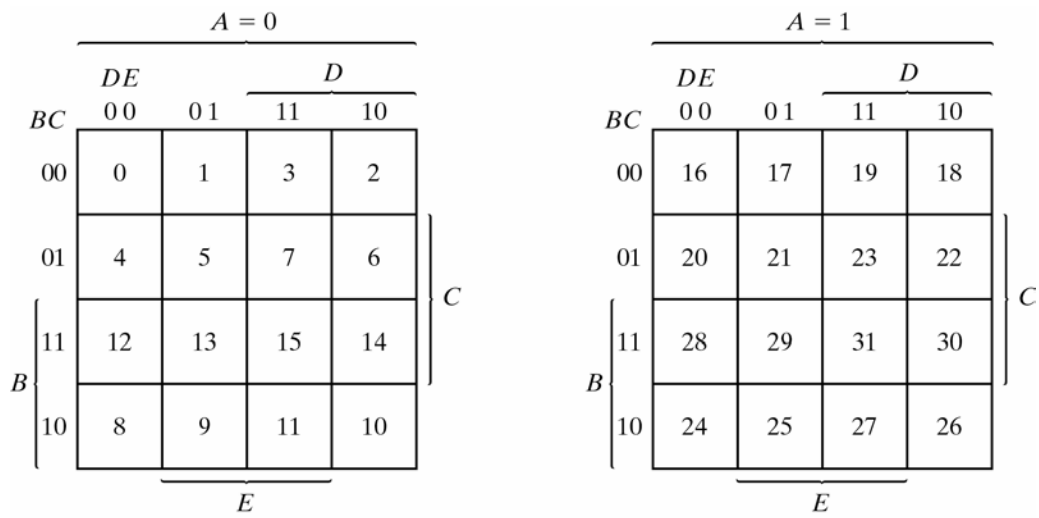


Fig. 3-12 Five-variable Map

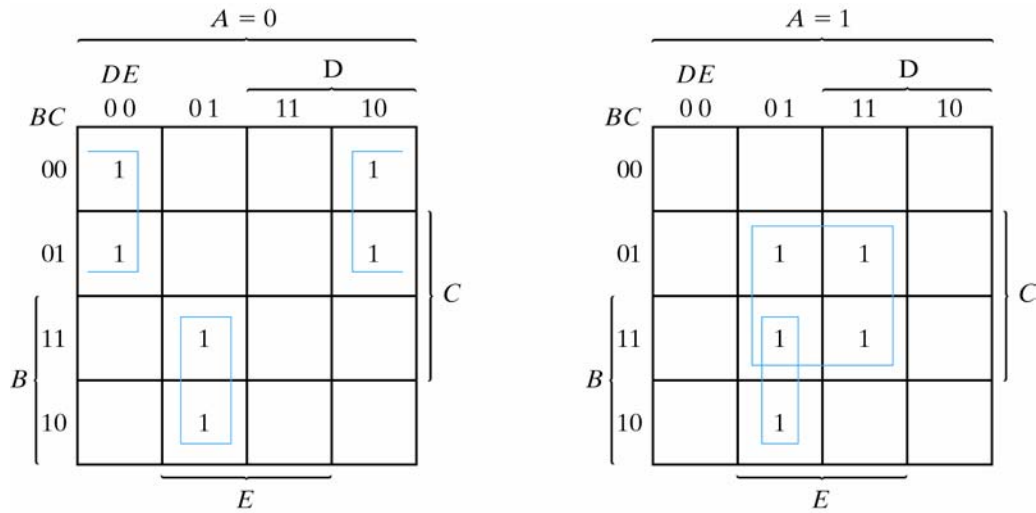
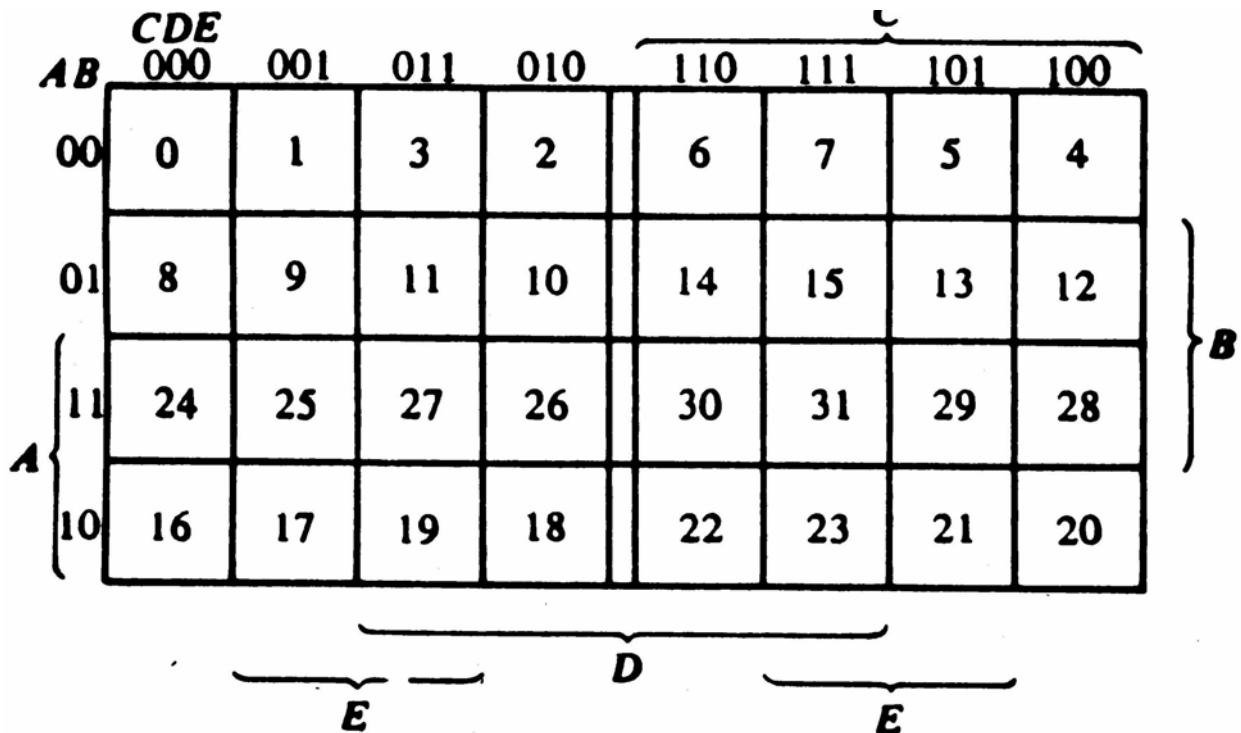


Fig. 3-13 Map for Example 3-7; $F = A'B'E' + BD'E + ACE$



ABC	DEF				D			
	000	001	011	010	110	111	101	100
000	0	1	3	2	6	7	5	4
001	8	9	11	10	14	15	13	12
011	24	25	27	26	30	31	29	28
010	16	17	19	18	22	23	21	20
110	48	49	51	50	54	55	53	52
111	56	57	59	58	62	63	61	60
101	40	41	43	42	46	47	45	44
100	32	33	35	34	38	39	37	36

Brackets on the right side of the table indicate groupings:

- Group C: {001, 011, 010, 111, 101, 100}
- Group B: {011, 010, 111, 101}
- Group C: {111, 101, 100}

Brackets at the bottom of the table indicate groupings:

- Group E: {011, 010, 111, 101}
- Group F: {001, 011, 111, 101}

AB	CD		C	
	00	01	11	10
00	1	1	0	1
01	0	1	0	0
11	0	0	0	0
10	1	1	0	1

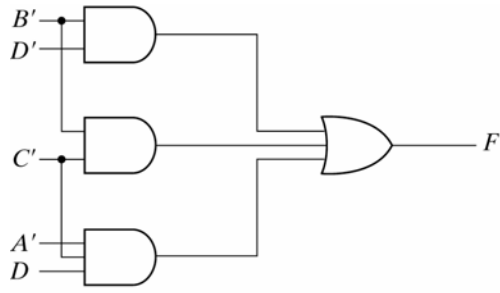
Brackets on the right side of the table indicate groupings:

- Group B: {01, 11, 10}

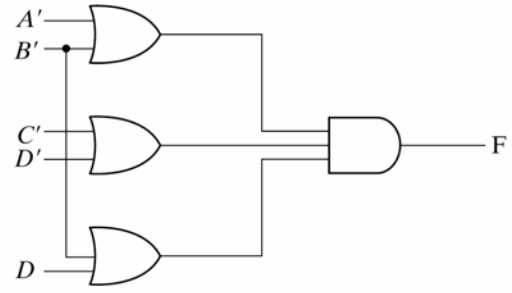
Brackets at the bottom of the table indicate groupings:

- Group D: {01, 11, 10}

Fig. 3-14 Map for Example 3-8; $F(A, B, C, D) = \Sigma(0, 1, 2, 5, 8, 9, 10)$
 $= B'D' + B'C' + A'C'D = (A' + B')(C' + D')(B' + D)$



(a) $F = B'D' + B'C' + A'C'D$



(b) $F = (A' + B')(C' + D')(B' + D)$

Fig. 3-15 Gate Implementation of the Function of Example 3-8

		yz		y	
		00	01	11	10
x	0	0	1	1	0
	1	1	0	0	1

z

Fig. 3-16 Map for the Function of Table 3-2

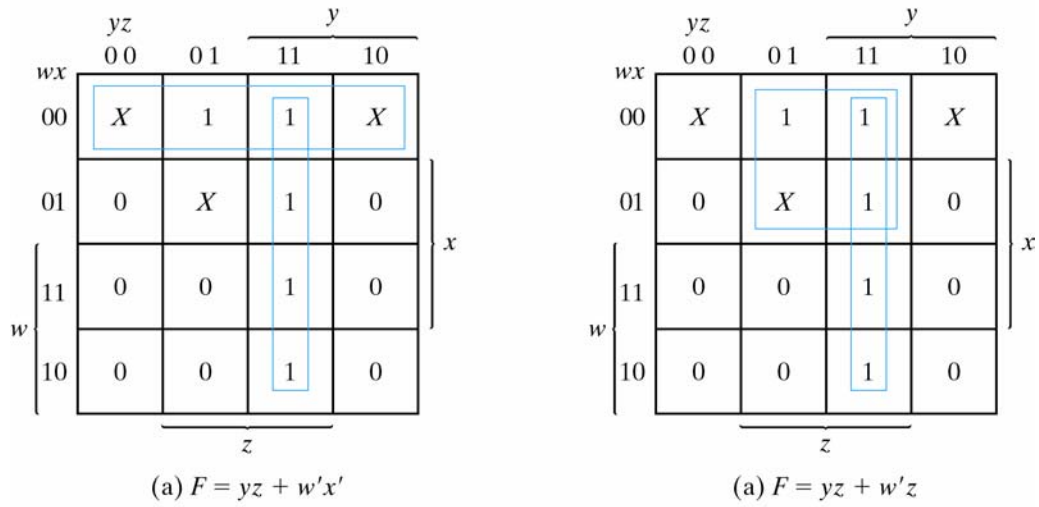


Fig. 3-17 Example with don't-care Conditions

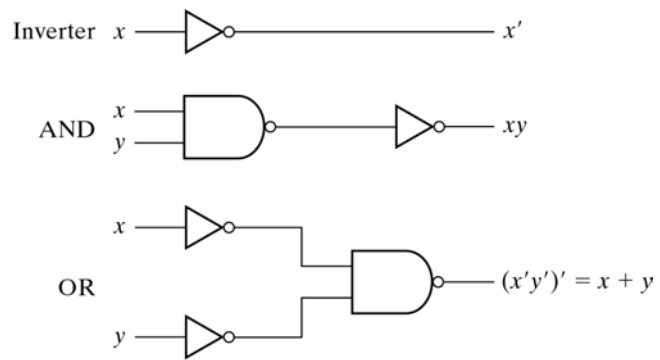


Fig. 3-18 Logic Operations with NAND Gates

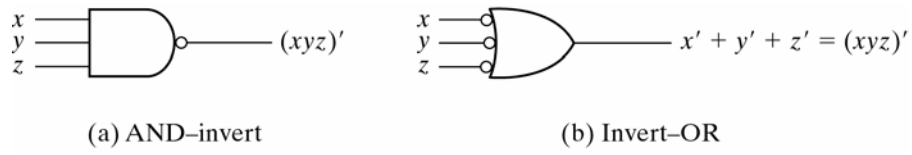


Fig. 3-19 Two Graphic Symbols for NAND Gate

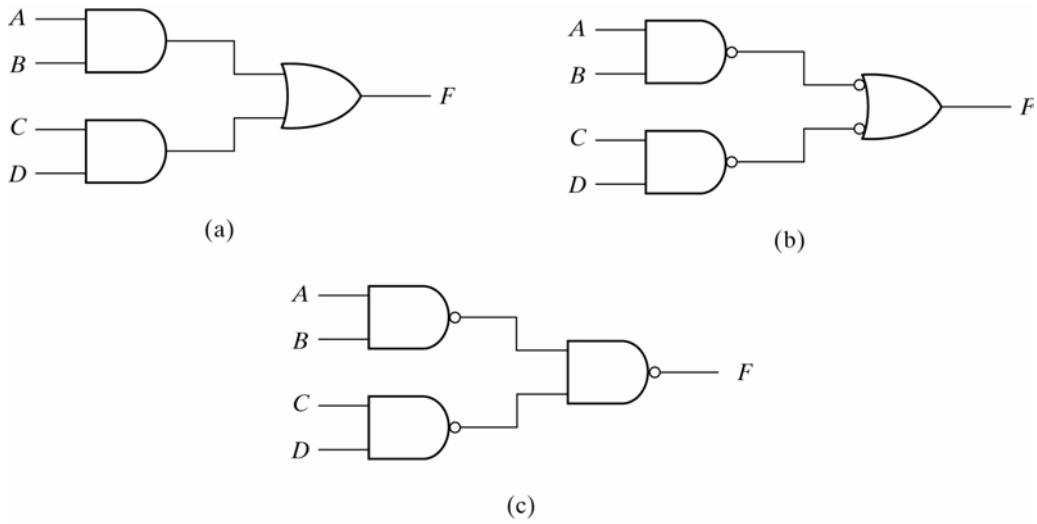


Fig. 3-20 Three Ways to Implement $F = AB + CD$

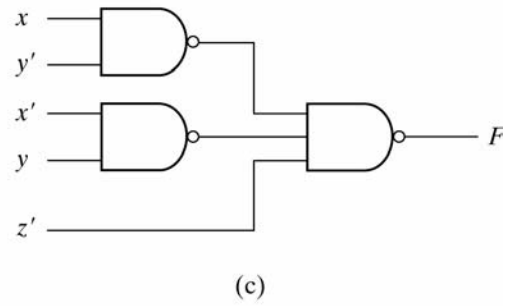
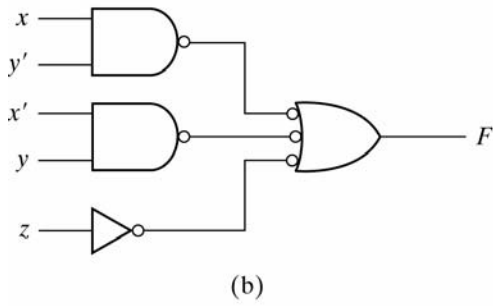
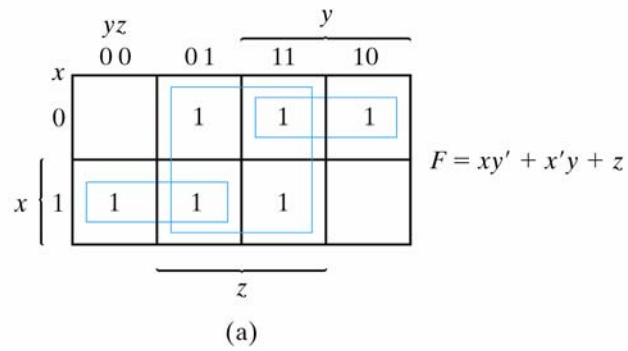


Fig. 3-21 Solution to Example 3-10

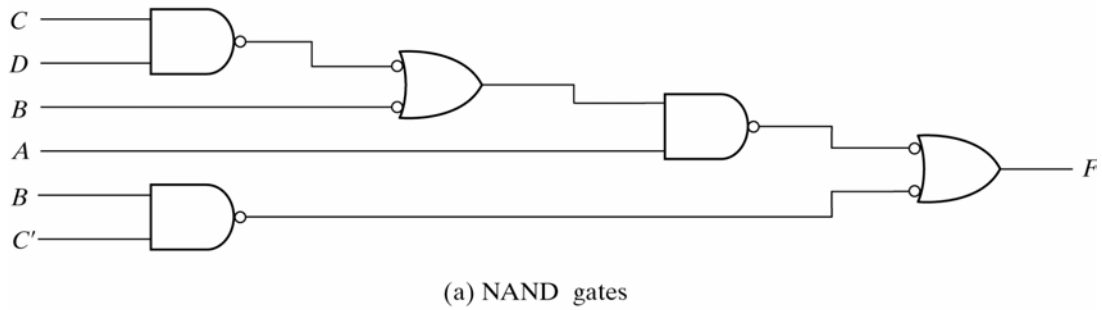
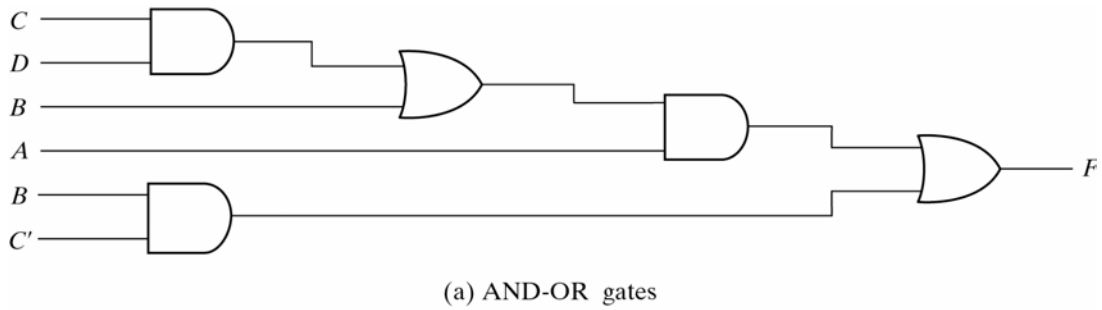
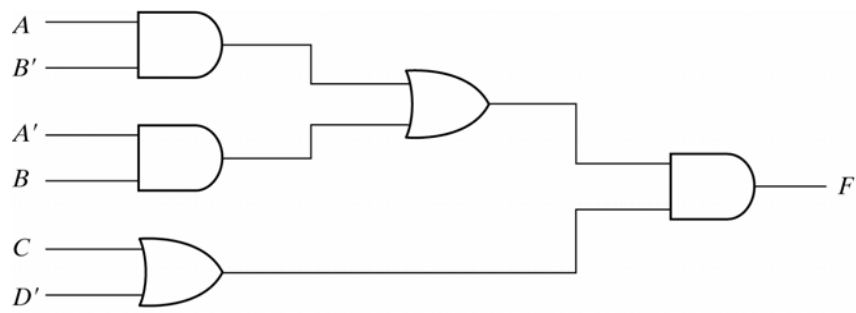
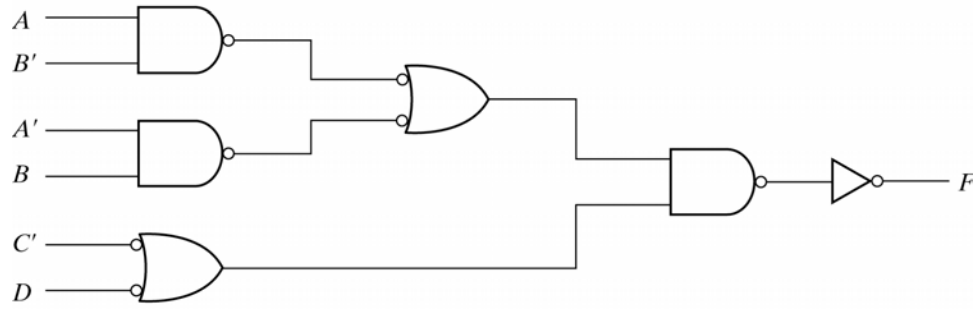


Fig. 3-22 Implementing $F = A(CD + B) + BC$



(a) AND-OR gates



(b) NAND gates

Fig. 3-23 Implementing $F = (AB' + A'B)(C + D')$

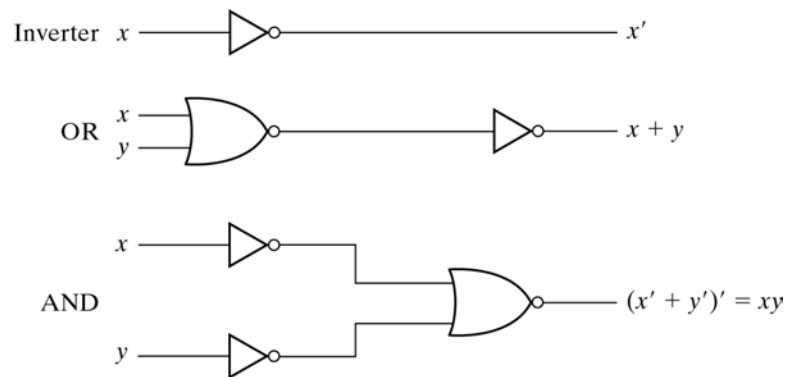
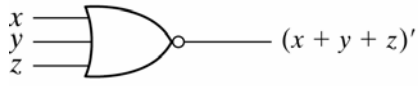
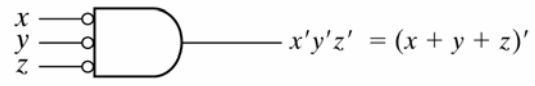


Fig. 3-24 Logic Operations with NOR Gates



(a) OR-invert



(a) Invert-AND

Fig. 3-25 Two Graphic Symbols for NOR Gate

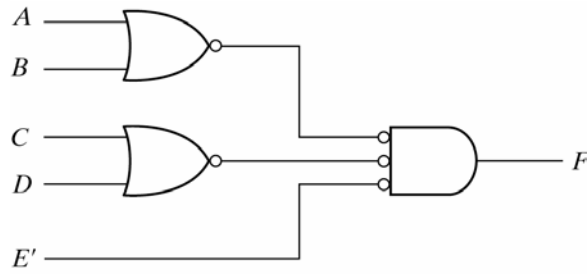


Fig. 3-26 Implementing $F = (A + B)(C + D)E$

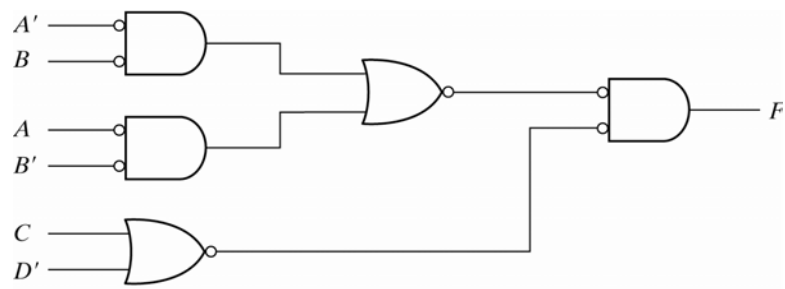
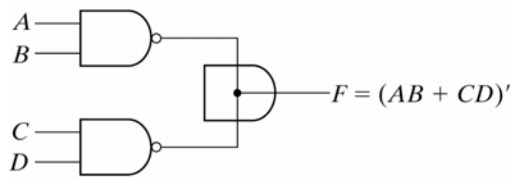
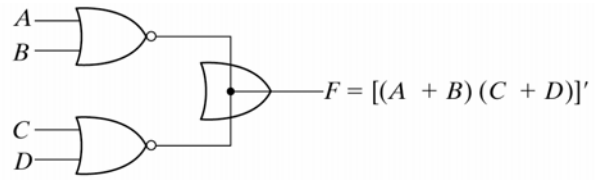


Fig. 3-27 Implementing $F = (AB' + A'B)(C + D')$ with NOR Gates

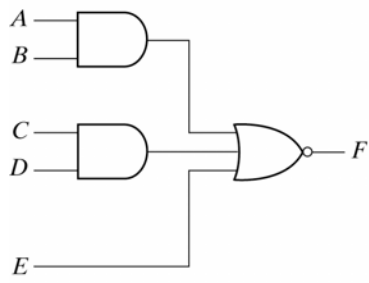


(a) Wired-AND in open-collector
TTL NAND gates.
(AND-OR-INVERT)

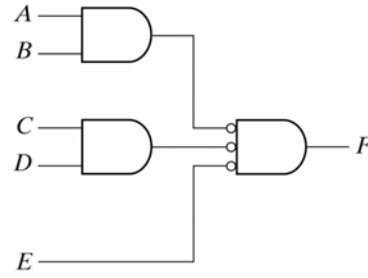


(b) Wired-OR in ECL gates
(OR-AND-INVERT)

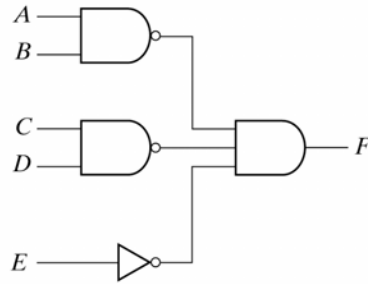
Fig. 3-28 Wired Logic



(a) AND-NOR

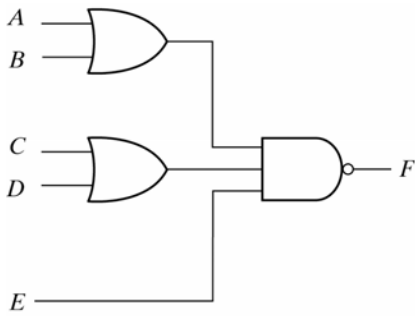


(b) AND-NOR

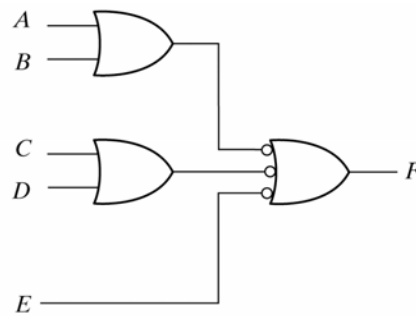


(c) NAND-AND

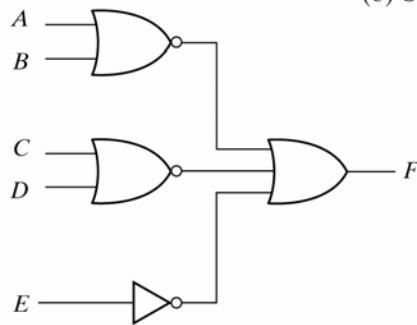
Fig. 3-29 AND-OR-INVERT Circuits; $F = (AB + CD + E)'$



(a) OR-NAND

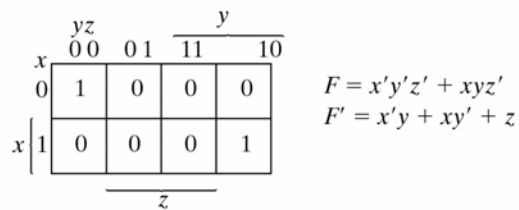


(b) OR-NAND

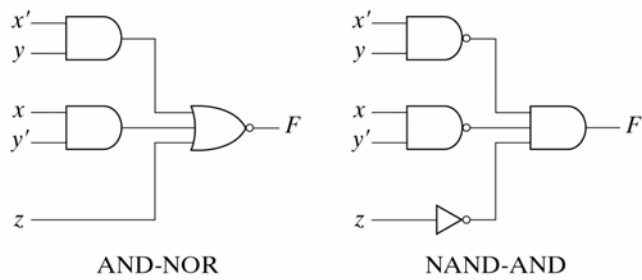


(c) NOR-OR

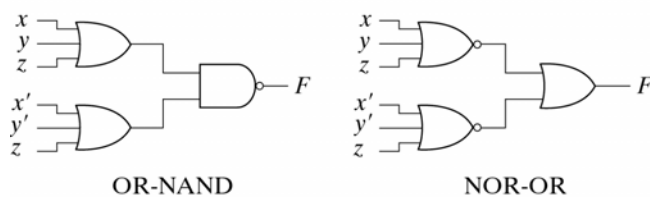
Fig. 3-30 OR-AND-INVERT Circuits; $F = [(A + B)(C + D)E]'$



(a) Map simplification in sum of products.

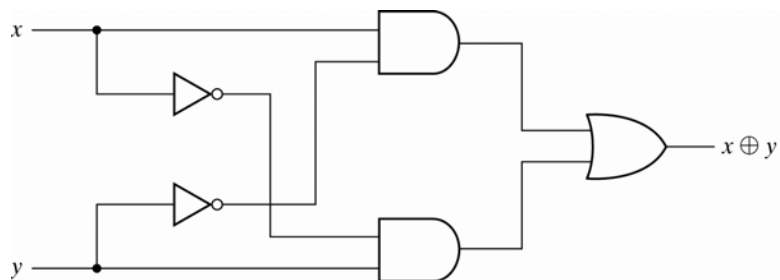


(b) $F = (x'y + xy' + z)'$

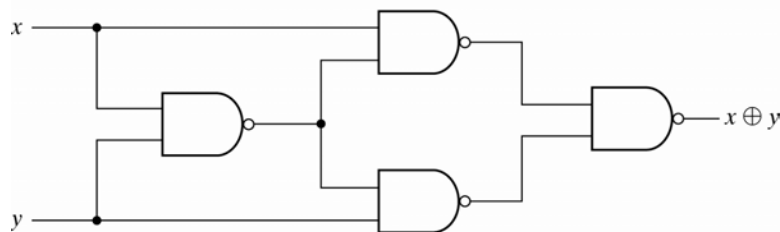


(c) $F = [(x + y + z)(x' + y' + z)]'$

Fig. 3-31 Other Two-level Implementations

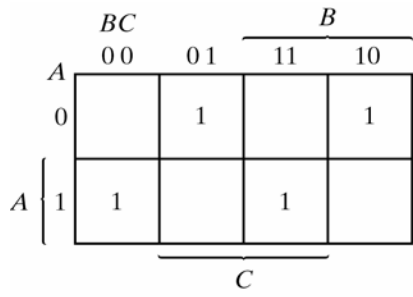


(a) With AND-OR-NOT gates

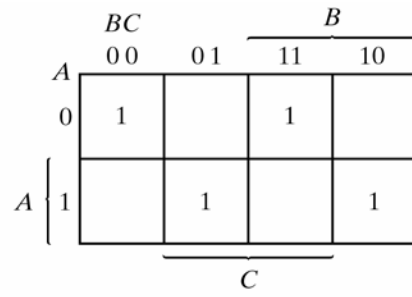


(b) With NAND gates

Fig. 3-32 Exclusive-OR Implementations

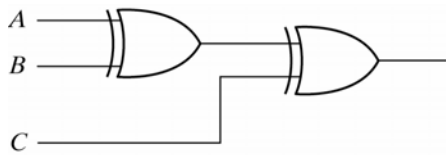


(a) Odd function
 $F = A \oplus B \oplus C$

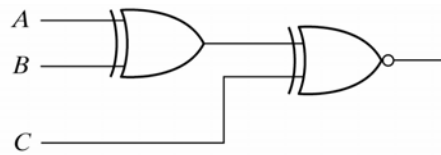


(a) Even function
 $F = (A \oplus B \oplus C)'$

Fig. 3-33 Map for a Three-variable Exclusive-OR Function



(a) 3-input odd function



(b) 3-input even function

Fig. 3-34 Logic Diagram of Odd and Even Functions

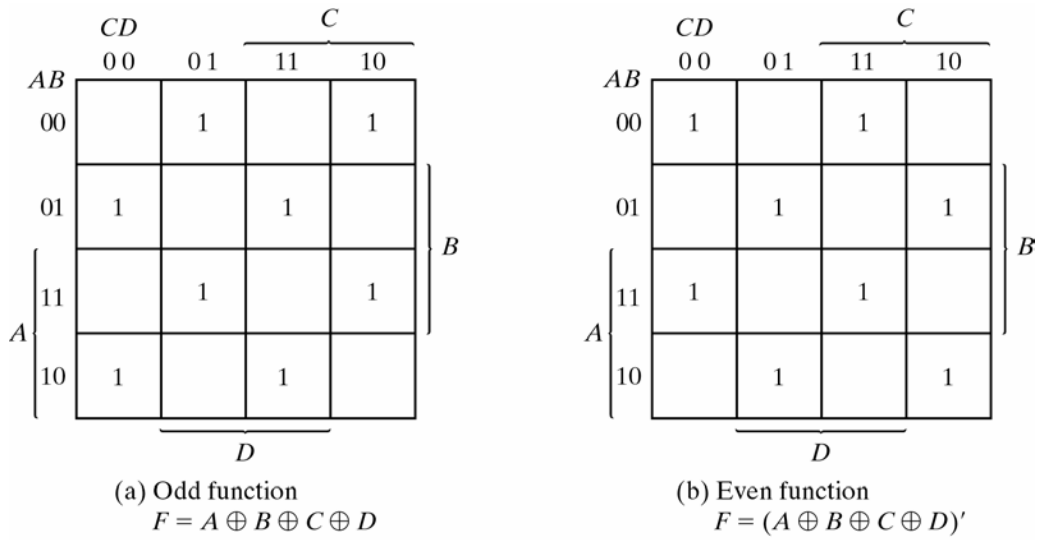


Fig. 3-35 Map for a Four-variable Exclusive-OR Function

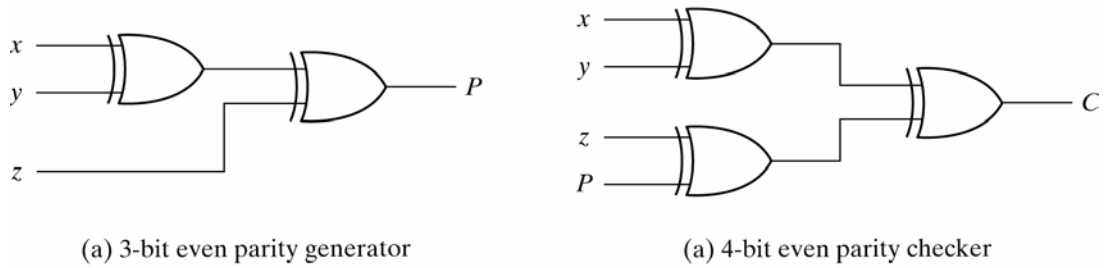


Fig. 3-36 Logic Diagram of a Parity Generator and Checker